

Final Review

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Final Review

- ❑ **Congratulations to All, you almost completed the ENGR 292 Fluids and Thermodynamics;**
- ❑ **Now it is time to do the final review.**

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Final Review

- ❑ **Let's check what we have achieved so far:**
 - **Topic: Fluid Mechanics, including Fluid Statics and Fluid Dynamics; Thermodynamics and Heat Transfer**
 - **Lectures: 20 Lectures**
 - **Assignments: 5 Assignments**
 - **Exam: 1 Midterm**

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Final Review

- ❑ **Today, we are going to have a final review to help you to review all you learnt so far before the final exam**
- ❑ **As usual, at the end of the semester, we will have a course evaluation**

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ENGR 292 Course Evaluations 2017W

- ❑ **Course Evaluation Instructions:**
 - **A sufficient amount of time will be set aside so that you as a student do not feel pressured to quickly complete these forms.**
 - **Ten to fifteen minutes is usually ample time to complete this process.**

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ENGR 292 Course Evaluations 2017W

- ❑ **Course Evaluation Instructions:**
 - **These course evaluation forms have been supplied to invite feedback from the students of ENGR 292 2017 W on your educational experience and on the College services provided to you.**

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ENGR 292 Course Evaluations 2017W

- **Course Evaluation Procedure:**
- 1) Assign one student in the class to retain this envelope.
 - 2) The assigned student will distribute one evaluation form to each student. Blank(s)/extra form(s) please leave in envelope.
 - 3) Once the students have completed the evaluations they should be returned to the assigned student.
 - 4) Seal envelope and bring envelope to the School of Trades and Technology Office-TEC 169
Attn: Aaron Vitaliano-Trades and Technology.

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Final Review

- **Fluid Mechanics (~40%)**
- Fluid Statics
 - Fluid Dynamics
- **Thermodynamics and Heat Transfer (~60%)**

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Evaluation

Assignments	30%	Note: • A weighted average of 50% must be attained on tests/examinations and a 50% must be attained on the final examination, otherwise an F will be awarded. • All assignments will have marks deducted; if handed in after assignments have been returned to the class, no mark will be given – but all assignments must be submitted in order to qualify to write the final exam
Midterm	30%	
Final	40%	

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Review of Fluid Statics

□ **Key Equations:**

- **Pressure**

$$P = \frac{F}{A}$$

- **Bulk Modulus**

$$E = \frac{-\Delta P}{\frac{\Delta V}{V}}$$

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Review of Fluid Statics

□ **Key Equations:**

- **Density**

$$\rho = \frac{m}{V}$$

- **Specific Weight**

$$\gamma = \frac{w}{V}$$

- **Specific Weight (γ) and Density (ρ) Relationship or $\gamma - \rho$ Relation:**

$$\gamma = \rho g$$

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Review of Fluid Statics

□ **Key Equations:**

- **Weight(w)-Mass(m) Relationship**

$$w = mg$$

- **Specific Gravity**

$$sg = \frac{\gamma_s}{\gamma_w@4^\circ\text{C}} = \frac{\rho_s}{\rho_w@4^\circ\text{C}}$$

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Review of Fluid Statics

□ Key Equations:

- **Dynamic Viscosity** ($\text{Pa} \cdot \text{s}$):

$$\eta = \frac{\tau}{\Delta v / \Delta y} = \tau \left(\frac{\Delta y}{\Delta v} \right)$$

- **Shear Stress** (Pa):

$$\tau = \eta \left(\frac{\Delta v}{\Delta y} \right)$$

- **Kinematic Viscosity** (m^2/s):

$$\nu = \frac{\eta}{\rho}$$

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Review of Fluid Statics

□ Key Equations:

- **Absolute and Gage Pressure**

$$P_{abs} = P_{gage} + P_{atm}$$

- **Pressure-Elevation Relationship**

$$\Delta p = \gamma h$$

- **Resultant force on a rectangular wall**

$$F_R = \gamma \left(\frac{h}{2} \right) A$$

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Review of Fluid Statics

□ Key Equations:

- **Resultant force on a submerged plane area**

$$F_R = \gamma h_c A$$

- **Location of Center of Pressure**

$$L_p = L_c + \frac{I_c}{L_c A}$$

- **Piezometric Head**

$$h_a = p_a / \gamma$$

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Review of Fluid Statics

□ Key Equations:

- **Buoyant force**

$$F_b = \gamma_f V_d$$

- **The distance to the metacenter from the Center of Buoyancy (MB)**

$$MB = I / V_d$$

- **Location of Metacenter:**

$$y_{mc} = y_{cb} + MB$$

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Review of Fluid Statics

□ Key Equations:

- **Metacentric Height (MG)**

$$MG = y_{mc} - y_{cg}$$

- **Stability of Floating Bodies**

If $y_{mc} > y_{cg}$, or if $MG > 0$, the floating body is stable

If $y_{mc} < y_{cg}$, or if $MG < 0$, the floating body is unstable

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Review of Fluid Dynamics

□ Key Equations:

- **Volume Flow Rate:**

$$Q = Av$$

- **Weight Flow Rate:**

$$W = \gamma Q$$

- **Mass Flow Rate:**

$$M = \rho Q$$

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Review of Fluid Dynamics

□ Key Equations:

- Continuity Equation for any Fluid:

$$\rho_1 A_1 v_1 = \rho_2 A_2 v_2$$

- Continuity Equation for Liquids:

$$A_1 v_1 = A_2 v_2$$

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Review of Fluid Dynamics

□ Key Equations:

- Bernoulli's Equation:

$$\frac{p_1}{\gamma} + z_1 + \frac{v_1^2}{2g} = \frac{p_2}{\gamma} + z_2 + \frac{v_2^2}{2g}$$

- Torricelli's Theorem:

$$v_2 = \sqrt{2gh}$$

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Review of Fluid Dynamics

□ Key Equations:

- General Energy Equation:

$$\frac{p_1}{\gamma} + z_1 + \frac{v_1^2}{2g} + h_A - h_R - h_L = \frac{p_2}{\gamma} + z_2 + \frac{v_2^2}{2g}$$

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Review of Fluid Dynamics

□ Key Equations:

- Reynolds Number – Circular Sections:

$$N_R = \frac{vD\rho}{\mu}$$

- Relative Roughness:

$$\frac{D}{\varepsilon}$$

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Review of Fluid Dynamics

□ Key Equations:

- Darcy's Equation for Energy Loss:

$$h_L = \left(f \frac{L}{D}\right) \frac{v^2}{2g}$$

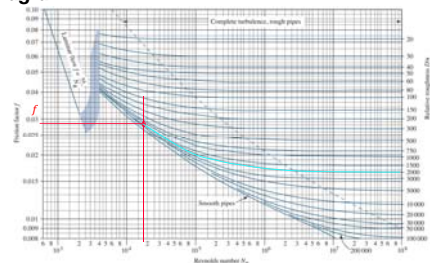
- Friction Factor for Laminar Flow

$$f = \frac{64}{N_R}$$

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Review of Fluid Dynamics

□ Friction Factor (f) for Turbulent Flow – Moody Diagram



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Review of Fluid Dynamics

□ **Key Equations:**

- **K Factor for Minor Losses:**

$$h_m = K \left(\frac{v^2}{2g} \right)$$

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Review of Fluid Dynamics

□ **Combined Head Loss Equation:**

$$h_L = \sum_{\text{pipes}} f \frac{L}{D} \frac{v^2}{2g} + \sum_{\text{components}} K \frac{v^2}{2g}$$

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Review of Fluid Dynamics

□ **Key Equations:**

- **Power Added to A Fluid by A Pump:**

$$P_A = h_A \gamma Q$$

- **Pump Efficiency:**

$$e_M = \frac{\text{Power delivered to fluid}}{\text{Power put into pump}} = \frac{P_A}{P_I}$$

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Review of Fluid Dynamics

□ **Key Equations:**

- **Power Removed from a Fluid by a Motor:**

$$P_R = h_R \gamma Q$$

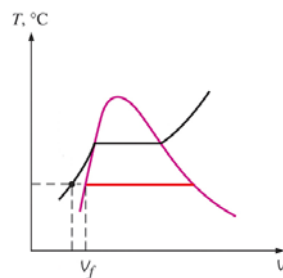
- **Motor Efficiency:**

$$e_M = \frac{\text{Power output from motor}}{\text{Power delivered by fluid}} = \frac{P_O}{P_R}$$

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Review of Thermodynamics

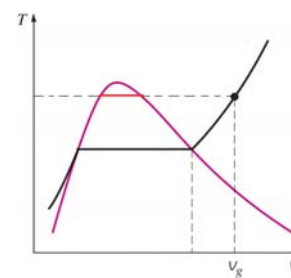
□ **Phase 1 - Compressed (Subcooled) Liquid**



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Review of Thermodynamics

□ **Phase 2 - Superheated Vapor**



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Review of Thermodynamics

□ **Phase 3 - Saturated Liquid-Vapor Mixture**
($0 < x < 1$)

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Review of Thermodynamics

□ **Phase 4 - Saturated Liquid** ($x = 0$)

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Review of Thermodynamics

□ **Phase 5 - Saturated Vapor** ($x = 1$)

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Review of Thermodynamics

□ **Entropy**

$$S_F - S_I = \int_I^F \left(\frac{dQ}{T} \right)_b + S_{gen}$$

$$S_{gen} \begin{cases} > 0 & \text{Irreversible Process} \\ = 0 & \text{Reversible Process} \\ < 0 & \text{Impossible Process} \end{cases}$$

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Review of Thermodynamics

□ **Entropy**

Isentropic – constant entropy processes
 $S_F - S_I = 0$

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Review of Thermodynamics

□ **Heat Engine (HE) and Ideal Rankine Cycle:**

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Review of Thermodynamics

□ **Heat Engine and Ideal Rankine Cycle:**

Process	
1-2	Isentropic Process
2-3	Isobaric Process
3-4	Isentropic Process
4-1	Isothermal & Isobaric Process

Phase	
1	Saturated Liquid ($x = 0$)
2	Compressed (Subcooled) Liquid
3	Superheated Vapor
4	Saturated Liquid-Vapor Mixture ($0 < x < 1$) Or Saturated Vapor ($x = 1$)

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Review of Thermodynamics

□ **Isentropic Efficiency**

Process	
1-2	Non-Isentropic Process
2-3	Isobaric Process
3-4	Non-Isentropic Process
4-1	Isothermal & Isobaric Process

Phase	
1	Saturated Liquid ($x = 0$)
2	Compressed (Subcooled) Liquid
3	Superheated Vapor
4	Saturated Liquid-Vapor Mixture ($0 < x < 1$) Or Saturated Vapor ($x = 1$)

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Review of Thermodynamics

□ **Isentropic Efficiency**

Devices	Isentropic Efficiency
Output device Turbine	$\eta_T = \frac{W_{T,Actual}}{W_{T,Ideal}} = \frac{h_3 - h_{4a}}{h_3 - h_{4s}} < 1$
Input device Pump	$\eta_P = \frac{W_{P,Ideal}}{W_{P,Actual}} = \frac{h_{2s} - h_1}{h_{2a} - h_1} < 1$

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Review of Thermodynamics

□ **Define the Properties (steam tables)**

State	T (°C)	P (MPa)	v (m³/kg)	h (kJ/kg)	s (kJ/(kgK))	Condition
1						
2						
3						
4						

□ Note: The data given is labeled by *

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Review of Thermodynamics

□ **Energy Analysis of the Heat Engine**

Energy Analysis	Equations
Net Work	$\dot{W}_{net out} = \dot{W}_T - \dot{W}_P$ $W_{net out} = Q_{in} - Q_{out}$
Heat Input	$Q_{in} = Q_B = \dot{m}_s(h_3 - h_4)$
Thermal Efficiency	$\eta = \frac{\dot{W}_{net out}}{Q_{in}} = \frac{\dot{W}_T - \dot{W}_P}{Q_{in}}$ $\eta = \frac{W_{net out}}{Q_{in}} = \frac{Q_{in} - Q_{out}}{Q_{in}} = 1 - \frac{Q_{out}}{Q_{in}}$

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Review of Thermodynamics

□ **Energy Analysis of the Heat Engine**

Energy Analysis	Equations
Net Power	$P_{net} = \dot{m}\dot{W}_{net out}$
Back Work Ratio	$\frac{\dot{W}_P}{\dot{W}_T}$

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Review of Thermodynamics

□ **Refrigeration (R) and Heat Pump (HP)**

Heat Pump: Heating effect is desired.

Refrigerator: Cooling effect is desired.

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Review of Thermodynamics

□ **Refrigeration (R) and Heat Pump (HP)**

Heat Pump: Heating effect is desired.

Refrigerator: Cooling effect is desired.

Process	
1-2	Isentropic Process
2-3	Isobaric Process
3-4	Isenthalpic Process
4-1	Isothermal & Isobaric Process

Phase	
1	Saturated Vapor ($x = 1$)
2	Superheated Vapor
3	Saturated Liquid ($x = 0$)
4	Saturated Liquid-Vapor Mixture ($0 < x < 1$)

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Review of Thermodynamics

□ **Define the Properties (Refrigerants tables)**

State	T (°C)	P (MPa)	v (m³/kg)	h (kJ/kg)	s (kJ/(kgK))	Condition
1						
2						
3						
4						

□ Note: The data given is labeled by *

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Review of Thermodynamics

□ **Refrigeration (R) and Heat Pump (HP)**

Energy Analysis	Equations
Compressor	$W_c = \dot{m}(h_2 - h_1)$
Expansion Valve	$h_3 = h_4 = h_{f4} + x(h_{g4} - h_{f4})$

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Review of Thermodynamics

□ **Refrigeration (R) and Heat Pump (HP)**

Energy Analysis			Equations
Condenser / Evaporator (Rejected)	R	Condenser	$\dot{Q}_{out} = \dot{m}(h_1 - h_4)$
	HP	Evaporator	$\dot{Q}_{in} = \dot{m}(h_2 - h_3)$
Condenser / Evaporator (Desired)	R	Evaporator	$\dot{Q}_{in} = \dot{m}(h_1 - h_4)$
	HP	Condenser	$\dot{Q}_{out} = \dot{m}(h_2 - h_3)$
Coefficients of Performance (COP)	R		$COP_R = \frac{\text{Cooling Effect}}{\text{Work Input}} = \frac{\dot{Q}_{in}}{W_c} = \frac{h_1 - h_4}{h_2 - h_1}$
	HP		$COP_{HP} = \frac{\text{Heating Effect}}{\text{Work Input}} = \frac{\dot{Q}_{out}}{W_c} = \frac{h_2 - h_3}{h_2 - h_1}$

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Review of Thermodynamics

□ **Thermal Efficiency (η) vs. Coefficients of Performance (COP)**

Energy Analysis			Equations
Thermal Efficiency (energy converting)			$\eta = \frac{W_{net\ out}}{\dot{Q}_{in}} = \frac{W_T - W_P}{\dot{Q}_{in}} = \frac{W_T - W_P}{h_1 - h_4} < 1$
			$\eta = \frac{W_{net\ out}}{\dot{Q}_{in}} = \frac{\dot{Q}_{in} - \dot{Q}_{out}}{\dot{Q}_{in}} = 1 - \frac{\dot{Q}_{out}}{\dot{Q}_{in}} < 1$
Coefficients of Performance (COP) (energy transferring)	R		$COP_R = \frac{\text{Cooling Effect}}{\text{Work Input}} = \frac{\dot{Q}_{in}}{W_c} = \frac{h_1 - h_4}{h_2 - h_1}$
	HP		$COP_{HP} = \frac{\text{Heating Effect}}{\text{Work Input}} = \frac{\dot{Q}_{out}}{W_c} = \frac{h_2 - h_3}{h_2 - h_1}$

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Review of Heat Transfer

□ **Key Equations:**

- **Conduction**

$$\dot{Q} = -kA \frac{dT}{dx}$$

$$\dot{Q} = -\frac{kA}{L} (T_2 - T_1)$$
- **Convection**

$$\dot{Q} = hA(T_s - T_\infty)$$

$$T_f = \frac{T_s + T_\infty}{2}$$

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Review of Heat Transfer

□ **To calculate the rate of heat transfer \dot{Q} :**

$$\dot{Q} = \frac{\Delta T}{R_{total}}$$

$$R_{Total} = \sum R_{Cond} + \sum R_{Conv}$$

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Review of Heat Transfer

□ **Thermal Resistance of Conduction**

Conduction Shape	R_{cond}	R	S
Plane Wall	$\frac{L}{kA}$	$\frac{1}{kS}$	$S = \frac{A}{L}$
Cylinder	$\frac{\ln(r_2/r_1)}{2\pi Lk}$	$\frac{1}{kS}$	$S = \frac{2\pi L}{\ln(r_2/r_1)}$
Sphere	$\frac{r_2 - r_1}{4\pi r_1 r_2 k}$	$\frac{1}{kS}$	$S = \frac{4\pi r_1 r_2}{r_2 - r_1}$
Others (Table 3-7)	$\frac{1}{kS}$	$\frac{1}{kS}$	

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Review of Heat Transfer

□ **Thermal Resistance of Convection:**

	$R_{Conv,in}$	$R_{Conv,out}$
Plane Wall	$\frac{1}{h_1 A}$	$\frac{1}{h_2 A}$
Cylinder	$\frac{1}{2\pi r_1 L h_1}$	$\frac{1}{2\pi r_2 L h_2}$
Sphere	$\frac{1}{4\pi r_1^2 h_1}$	$\frac{1}{4\pi r_2^2 h_2}$

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Review of Heat Transfer

□ **To find conductive heat transfer coefficient k , just to look up its value in the tables, because it is the property of a material.**

Material	Thermal Conductivity k W/m °C
Metals:	
Silver (pure)	410
Copper (pure)	385
Aluminum (pure)	202
Nickel (pure)	92
Iron (pure)	73
Carbon steel, 1% C	62
Lead (pure)	35
Chrome-nickel steel (18% Cr, 8% Ni)	16.3
Nonmetallic Solids:	
Quartz, fused (in vac)	41.6
Magnesium	4.51
Alumina	2.08-2.04
Silicon	1.81
Glass, window	0.78
Aluminum Oxide	0.27
Stainless	0.039
Glass wool	0.038
Liquids:	
Mercury	8.21
Water	0.256
Ammonia	0.254
Lubricating oil, SAE 50	0.147
Freon 12, CCl ₄	0.073
Gases:	
Hydrogen	0.178
Helium	0.141
Air	0.024
Water vapor (saturated)	0.0206
Carbon dioxide	0.018

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Review of Heat Transfer

□ **Determine the convective heat transfer coefficient h is not an easy task. Convection Heat Transfer Coefficient (h) is not a property of the material.**

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Review of Heat Transfer

- Use Patterns defined in Table C-8 to calculate Nu to determine h

$$h = \frac{(Nu)k}{L}$$

- by calculating Re for forced convection
- by calculating Gr for natural convection

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Review of Heat Transfer

- **Forced Convection**
- Fluid was forced to move over a surface or in a tube by external means such as a pump or a fan.

Table C-8

- (A) Flow in circular tubes
 (B) Boundary layer on a flat plate
 (C) Single circular cylinder or sphere in cross flow

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Review of Heat Transfer

- **Natural Convection**
- Any fluid motion occurs by natural means such as buoyancy

Table C-8

- (D) Natural convection from a horizontal cylinder
 (E) Natural convection from vertical surfaces

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Review of Heat Transfer

- **Procedure for Calculating “h” – Forced Convection:**
1. Determine the geometric parameter L ;
 2. Determine the type of the Forced Convection in Table C-8 (A), (B) or (C)
 3. Assume a fluid temperature, T_f (°K) (if it is not given). Look up the thermo-physical properties (ρ, k, μ, ν, Pr) of the fluid used in the convection in Table A-18 (if Pr is not given, use $Pr = \frac{\mu C_p}{k}$)

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Review of Heat Transfer

4. Calculate the Reynolds number (Re) or other information to determine the Flow type – Laminar or Turbulent

$$Re = \frac{vL\rho}{\mu} = \frac{vL}{\nu}$$

Please note:

Critical Reynolds Numbers

- Inside a Pipe
 - $Re_{cr} = 2000$
- Over a Flat Plate
 - $Re_{cr} = 500,000$

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Review of Heat Transfer

5. Calculate Nusselt number (Nu)

$$Nu = C Re_L^m Pr^n$$

Find C, m, n as per flow type and thermal boundary layer condition

6. Calculate h

$$h = \frac{(Nu)k}{L}$$

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Review of Heat Transfer

□ Procedure for Calculating “h” – Natural Convection:

1. Determine the geometric parameter L ;
2. Determine the type of the Natural Convection in Table C-8 (D) or (E)
3. Assume a fluid temperature, T_f ($^{\circ}\text{K}$) (if it is not given). Look up the thermo-physical properties (ρ, k, μ, ν, Pr) of the fluid used in the convection in Table A-18

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Review of Heat Transfer

□ 4. Calculate the Grashof number (Gr)

$$Gr = \frac{g\beta(T_{\text{surface}} - T_{\infty})L^3\rho^2}{\mu^2}$$

$$\beta = \frac{1}{T_f} \quad \text{for gas only } (K = C + 273.15)$$

5. Calculate Nusselt number (Nu)

$$Nu = C(Gr \times Pr)^n$$

Find C and n as per the value of $(Gr \times Pr)$

6. Calculate h

$$h = \frac{(Nu)k}{L}$$

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Review of Heat Transfer

□ Key Equations:

- Fin Efficiency

$$\eta_{Fin} = \frac{\dot{Q}_{Fin}}{\dot{Q}_{Fin,Max}}$$

$$\dot{Q}_{Fin,Max} = hA_{Fin}(T_b - T_{\infty})$$

$$A_{Fin} = A_{Fin,Sides} + A_{Fin,Tip}$$

$$\dot{Q}_{Fin} = \eta_{Fin}\dot{Q}_{Fin,Max}$$

$$= \eta_{Fin}hA_{Fin}(T_b - T_{\infty})$$

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Review of Heat Transfer

□ Key Equations:

- Fin Effectiveness

$$\varepsilon_{Fin} = \frac{\dot{Q}_{Fin}}{\dot{Q}_{No\ Fin}}$$

$$= \frac{\eta_{Fin}hA_{Fin}(T_b - T_{\infty})}{hA_b(T_b - T_{\infty})} = \frac{\eta_{Fin}A_{Fin}}{A_b}$$

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Review of Heat Transfer

□ Key Equations:

- Multiple Fins:

$$\dot{Q}_{Total\ Fin} = \dot{Q}_{UnFin} + \dot{Q}_{Fin}$$

$$= h(A_{UnFin} + \eta_{Fin}A_{Fin})(T_b - T_{\infty})$$

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Review of Heat Transfer

□ Heat Sink Selection:

$$R_{required} = \frac{\Delta T}{\dot{Q}}$$

Selection Criteria:

$$R_{Heat\ Sink} < R_{required}$$

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Final Exam Information

- ENGR 292 Final Exam is a closed book exam. However, the Cheat Sheet is allowed in the final exam. Here is the detail information about the Cheat Sheet:

You may bring two double-sided 8½"×11" sheet of paper with anything you like written on both sides (Four single-sided sheets are okay). However, Cheat sheets must be hand-written, not photocopied or printed.

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Final Exam Information

- What will be provided in the Final Exam if needed:
 - Unit Conversion Factors
 - Material Properties, such as density, viscosity, etc.
 - Properties of Areas
 - Dimensions of Steel Pipes
 - Pipe Roughness
 - Moody Diagram
 - Figures and Tables of K Factors of Minor Losses

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Final Exam Information

- What will be provided in the Final Exam if needed:
 - Thermal Conductivity k
 - Table 3-7 Conduction Shape Factor S for Common Configurations
 - Table C-8 for convective heat transfer coefficient h
 - Steam Tables & R134a Properties
 - Figures 8-59 & 8-60 for Finned Surface Heat Transfer
 - Table 8-6 for Heat Sink Selection

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Final Exam Information

- You are permitted to use your own calculator, but you are not permitted to store any course-related information in your calculator and to use it.
- Cell phone is not allowed in the Final Exam.

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Final Exam Information

- Organize yourself before the Final Exam:
 - Use course objective to study
 - Review the ENGR 292 Website and ENGR 292 D2L; Read through the notes, examples, tutorials etc.
 - Review your assignments and against the posted solutions.

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Final Exam Information

- Organize yourself before the Final Exam:
 - Prepare your cheat sheet
 - Concepts
 - Key Equations
 - Make sure to remember: Circle Area: $A = \pi r^2 = \frac{\pi D^2}{4}$
 - Anything you think is important

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Final Exam Information

- **During the Final Exam:**
 - **Show your work:**
 - Numerical Questions: make sure to show your work!
 - Descriptive Questions: answer clearly and concisely. Spelling and Grammar count!
 - **Budget your time:** Look at how much each question is worth.
 - **Attempt all the questions.** You do not have to do questions in numerical order.
 - **Do not get stuck on one question**
 - **Do not leave any answers blank**
 - **Good Luck !**

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What is Next?

- **Apr.07 No Class**
 - **Reading Assignment**
 - **Assignment 5**

- **Apr.11, Self-Study or Questions time?**

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What is Next?

- **Final Exam (3 hrs):**
 - **Time: Apr.18, 18:00 pm – 21:00 pm**
 - **Location: CBA 285**

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