

Energy

Fundamental concept of thermodynamics.

One of the *most significant aspects* of engineering analysis.

Create list examples of energy generation or consumption in our daily lives

Conservation of Energy:

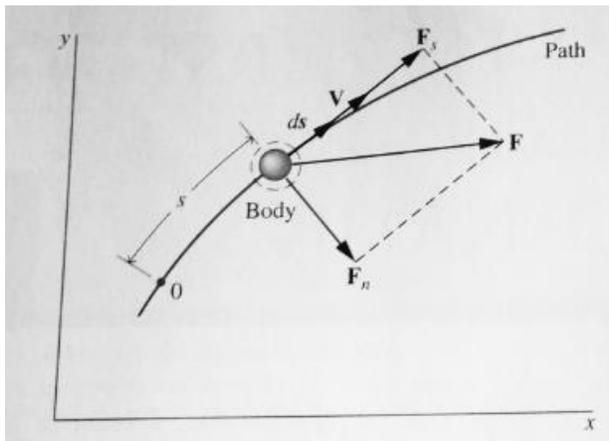
- The total amount of energy in the system is conserved

Energy can be: *stored, transformed or transferred*

Newton formulated a general description of motion under applied forces, which led to the concepts of:

- Work
- Kinetic Energy
- Potential Energy

Nomenclature



Where:

- F = force acting on the body in motion
- F_s = force component along path or 'streamline'. Affects **magnitude**.
- F_n = force component normal to the path. Affects **direction**.
- $F = F\{s\}$

$$F_s = m \frac{dv}{dt}$$

$$F_s = m \frac{dv}{ds} \frac{ds}{dt} = mv \frac{dv}{ds} \quad \rightarrow \text{Work}$$

$$\int_{v_1}^{v_2} mv dv = \int_{s_1}^{s_2} F_s ds \quad \rightarrow \text{Kinetic energy}$$

$$\int_{v_1}^{v_2} mv dv = \left. \frac{1}{2} mv^2 \right|_{v_1}^{v_2} = \frac{1}{2} m(v_2^2 - v_1^2)$$

Kinetic Energy: Change in kinetic energy = $\frac{1}{2}m(v_2^2 - v_1^2)$

Work: The work of the resultant force on the body equals the change in it's kinetic energy.

Units

- Metric = $N \cdot m = J$
- Imperial = Btu

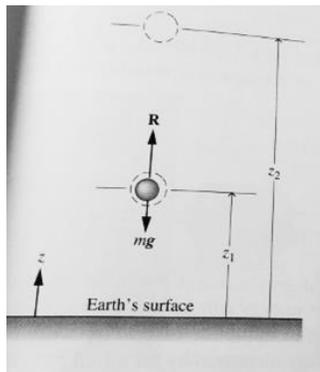
General equation:

$$\frac{1}{2}m(v_2^2 - v_1^2) = \int_{s_1}^{s_2} F \cdot ds$$

Work done by the body can be considered a transfer of energy to the body, where it is stored as kinetic energy.

Potential Energy

The energy that an object has due to its position in a force field or that a system has due to the configuration of its parts.



Where:

- mg = force due to gravity
- R = resultant of all other forces acting on the system

Apply governing equation for multiple forces in the z direction:

$$\frac{1}{2}m(v_2^2 - v_1^2) = \int_{z_1}^{z_2} R \cdot dz - \int_{z_1}^{z_2} mg \cdot dz$$

$$\int_{z_1}^{z_2} mg \cdot dz = mg(z_2 - z_1)$$

Therefore:

$$\frac{1}{2}m(v_2^2 - v_1^2) + mg(z_2 - z_1) = \int_{z_1}^{z_2} R \cdot dz$$

Gravitational potential energy = mgz

Work

$$W = \int_{s1}^{s2} F \cdot ds$$

A means of transferring energy

Work is done by a system on it's surroundings if the sole effect on everything external to the system *could have been* the raising of a weight.

This is very analogous to mechanics.

Sign conventions:

- $W > 0$: Work is done *by* the system
- $W < 0$: Work is done *on* the system

Power

The rate of energy transfer by work = \dot{W} or P

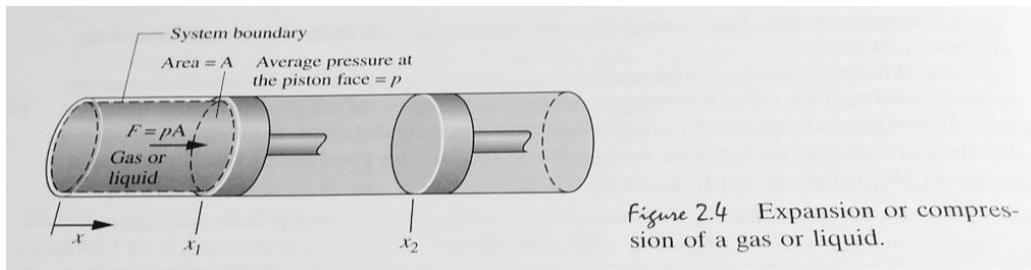
$$\dot{W} = F \cdot v$$

Therefore

$$W = \int_{t1}^{t2} \dot{W} dt = \int_{t1}^{t2} F \cdot v dt$$

Expansion or Compression Work

Piston -cylinder assembly



$$\delta W = pAdx = pdV$$

$$W = \int_{V1}^{V2} pdV$$

Power Transmitted by a Shaft

A rotating shaft with angular velocity, ω , and exerting a torque, T , on it's surroundings produces the following power:

$$\dot{W} = F_t v = \left(\frac{T}{R}\right) (R\omega) = \omega T$$

Where:

- R = radius
- F_t = tangential force
- n = shaft speed

$$\dot{W} = 2\pi n T$$

First Law of Thermodynamics

The law of conservation of energy states that **the total energy of an isolated system is constant**; energy can be transformed from one form to another, but cannot be created or destroyed.

Adiabatic process - No thermal interactions between the system and it's surroundings

Change in energy between two states: $E_2 - E_1 = -W_{ad}$

Where W_{ad} = net work for any adiabatic process between two states. Negative sign means work done *on* the system.

Internal Energy

E denotes total energy, including kinetic, potential energy, and others. These 'others' are considered internal energy, U .

Examples of internal energy:

1. Compress a spring
2. Charge a battery
3. Others?

Therefore, the change in total energy of the system is defined as:

$$\Delta E = \Delta KE + \Delta PE + \Delta U \text{ (for an adiabatic process)}$$

Heat Transfer

Non-Adiabatic Process - A process that involves a thermal interaction between a system and it's surroundings.

Energy transfer Q is only induced as a result of temperature difference between the system and the surroundings and only occurs in the direction of decreasing temperature. *Energy transfer by heat.*

$$Q = (E_2 - E_1) + W, \text{ or}$$

$$\Delta KE + \Delta PE + \Delta U = Q - W$$

$$\left[\begin{array}{c} \text{change in the amount} \\ \text{of energy contained} \\ \text{within the system} \\ \text{during some time} \\ \text{interval} \end{array} \right] = \left[\begin{array}{c} \text{net amount of energy} \\ \text{transferred in across} \\ \text{the system boundary by} \\ \text{heat transfer during} \\ \text{the time interval} \end{array} \right] - \left[\begin{array}{c} \text{net amount of energy} \\ \text{transferred out across} \\ \text{the system boundary} \\ \text{by work during the} \\ \text{time interval} \end{array} \right]$$

Sign conventions (opposite of work):

- $Q > 0$: heat transfer *to* the system
- $Q < 0$: heat transfer *from* the system

Heat transfer rate, \dot{Q} , is the amount of heat transfer per unit time. $Q = \int_{t_1}^{t_2} \dot{Q} dt$

Heat flux: $\dot{Q} = \int_A \dot{q} dA$, where \dot{q} is heat transfer per unit area.

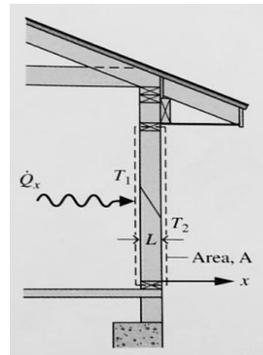
Heat Transfer Mechanisms

Conduction: Energy transfer in solids, liquids or gases. The rate of heat transfer across any plane normal to the x direction, \dot{Q}_x , is proportional to the wall area, A and temperature gradient in the x direction.

$$\dot{Q}_x = -kA \left[\frac{T_2 - T_1}{L} \right]$$

Where:

- k = thermal conductivity (available in tables)
- L is the wall thickness



Thermal radiation: Emitted by mater as a result of changes in the electronic configuration of the atoms or molecules within it.

Energy is transported by electromagnetic waves. No intervening medium is required and can therefore occur in a vacuum.

$$\dot{Q}_e = \epsilon \sigma A T_b^4$$

Where:

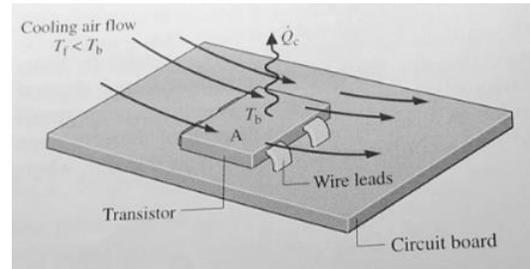
- T_b is temperature of the surface
- ϵ is the emissivity, a property of the surface. How effectively it radiates.
- σ is the Stefan-Boltzmann constant.
- Highly sensitive to temperature, T_b

Convection: Energy transfer between a solid surface at T_b and the adjacent moving gas or liquid at temperature T_f .

$$\dot{Q}_c = hA(T_b - T_f)$$

Where:

- h is the heat transfer coefficient



Forced convection - when fans or pumps cause the fluid to move

Natural convection - buoyancy induced motion

Applications	h (W/m ² ·K)	h (Btu/h · ft ² · °R)
Free convection		
Gases	2–25	0.35–4.4
Liquids	50–1000	8.8–180
Forced convection		
Gases	25–250	4.4–44
Liquids	50–20,000	8.8–3500

So what comes next?

1. Control volume energy analysis
 - a. Open systems with energy transfer through a moving fluid
 - b. Application of continuity and energy balance
2. Property relations
3. Thermodynamic cycles