

ENGR 292 Fluids and Thermodynamics

Scott Li, Ph.D., P.Eng.
Mechanical Engineering Technology
Camosun College

Mar.10, 2017

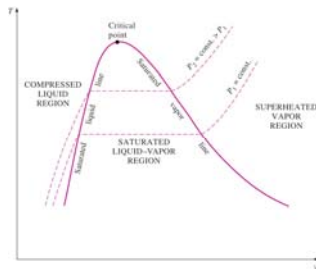
Review of Last Class

- T-v diagram
- P-v diagram
- Steam Table

2

Review of Last Class

- T-v diagram



3

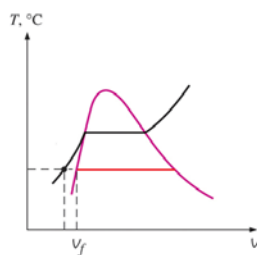
Review of Last Class

- **Compressed (Subcooled) Liquid**
 - Higher pressure ($P > P_{sat}$ at a given T)
 - Lower temperature ($T < T_{sat}$ at a given P)
 - Lower specific volume ($v < v_f$ at a given P or T)
 - Lower internal energy ($u < u_f$ at a given P or T)
 - Lower enthalpies ($h < h_f$ at a given P or T)

4

Review of Last Class

- **Compressed (Subcooled) Liquid**



5

Review of Last Class

- **Superheated Vapor**
 - Lower pressure ($P < P_{sat}$ at a given T)
 - Higher temperature ($T > T_{sat}$ at a given P)
 - Higher specific volume ($v > v_g$ at a given P or T)
 - Higher internal energy ($u > u_g$ at a given P or T)
 - Higher enthalpies ($h > h_g$ at a given P or T)

6

Review of Last Class

□ **Superheated Vapor**

7

Review of Last Class

□ **Saturated Liquid-Vapor Mixture**

- Saturated pressure ($P = P_{sat}$ at a given T)
- Saturated temperature ($T = T_{sat}$ at a given P)
- Quality $0 < x < 1$
- Specific volume ($v_f < v < v_g$)
- Internal energy ($u_f < u < u_g$)
- Higher enthalpies ($h_f < h < h_g$)

8

Review of Last Class

□ **Saturated Liquid-Vapor Mixture ($0 < x < 1$)**

9

Review of Last Class

□ **Saturated Liquid ($x = 0$)**

10

Review of Last Class

□ **Saturated Vapor ($x = 1$)**

11

Review of Last Class

□ **Enthalpy – A Combination Property**

Total Enthalpy

$$H = U + PV$$

Specific Enthalpy (per unit mass):

$$h = u + Pv$$

12

Total Energy of a Flowing Fluid

- The total energy of a flowing fluid on a unit-mass basis (denoted by θ , methalpy)

$$\begin{aligned}\theta &= Pv + u + ke + pe \\ &= Pv + u + \frac{v^2}{2} + gz \\ &= h + \frac{v^2}{2} + gz \text{ (kJ/kg)}\end{aligned}$$

13

Energy Transferred by Heat

- Amount of Heat transferred is denoted by Q (kJ)
- Heat transfer per unit mass is denoted by $q = \frac{Q}{m}$ (kJ/kg)
- Rate of Heat Transfer (the amount of heat transferred per unit time) is denoted by \dot{Q} (kJ/s) or (kW)

14

Energy Transferred by Work

- The work done during a process is denoted by W (kJ)
- Work done per unit mass is denoted by $w = \frac{W}{m}$ (kJ/kg)
- The work done per unit time is denoted by \dot{W} (kJ/s) or (kW)

15

Energy Transported by Mass

- Amount of Energy Transport:

$$E_{\text{mass}} = m\theta = m \left(h + \frac{v^2}{2} + gz \right) \text{ (kJ)}$$

- Rate of Energy Transport:

$$\dot{E}_{\text{mass}} = \dot{m}\theta = \dot{m} \left(h + \frac{v^2}{2} + gz \right) \text{ (kW)}$$

16

Energy Transported by Mass

- If the kinetic and potential energies of a fluid stream are negligible, then

- Amount of Energy Transport:

$$E_{\text{mass}} = mh \text{ (kJ)}$$

- Rate of Energy Transport:

$$\dot{E}_{\text{mass}} = \dot{m}h \text{ (kW)}$$

17

The First Law of Thermodynamics

- The first law of thermodynamics is simply a statement of the conservation of energy principle.

- The general energy balance:

$$E_{\text{in}} - E_{\text{out}} = \Delta E_{\text{system}}$$

18

The First Law of Thermodynamics

- **The general energy balance:**

$$E_{in} - E_{out} = \Delta E_{system}$$

$$\begin{aligned} E_{in} - E_{out} \\ = (Q_{in} - Q_{out}) + (W_{in} - W_{out}) \\ + (E_{massin} - E_{massout}) = \Delta E_{system} \end{aligned}$$

19

Some Steady-Flow Engineering Devices

A large number of engineering devices such as

- Nozzle
- Turbine
- Compressor
- Heat Exchanger
- Valve

Operates for long periods of time under same conditions, and they classified as steady flow devices.

20

Steady Flow Systems

- **Energy balance for steady-flow systems**

- **The general energy balance:**

$$E_{in} - E_{out} = \Delta E_{system}$$

21

Some Steady-Flow Engineering Devices

- **All the devices have steady mass flow through them**

$$\frac{dm_{cv}}{dt} = 0$$

- **And there is no change in stored energy**

22

Some Steady-Flow Engineering Devices

Therefore

$$\frac{\dot{Q}_{cv}}{\dot{m}} - \frac{\dot{W}_{cv}}{\dot{m}} + (h_i - h_e) + \frac{v_i^2 - v_e^2}{2} + g(z_i - z_e) = 0$$

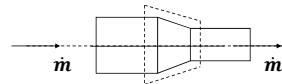
Where: **cv = control volume**

i = inlet

e = exit

23

Nozzle



$$\frac{\dot{Q}_{cv}}{\dot{m}} - \frac{\dot{W}_{cv}}{\dot{m}} + (h_i - h_e) + \frac{v_i^2 - v_e^2}{2} + g(z_i - z_e) = 0$$

$$(h_i - h_e) + \frac{v_i^2 - v_e^2}{2} = 0$$

24

Turbine

$$\frac{\dot{Q}_{cv}}{\dot{m}} - \frac{W_{cv}}{\dot{m}} + (h_i - h_e) + \frac{v_i^2 - v_e^2}{2} + g(z_i - z_e) = 0$$

$$-\frac{W_{cv}}{\dot{m}} + (h_i - h_e) = 0$$

$$W_{out} = W_{cv}$$

25

Compressor (Pump)

$$\frac{\dot{Q}_{cv}}{\dot{m}} - \frac{W_{cv}}{\dot{m}} + (h_i - h_e) + \frac{v_i^2 - v_e^2}{2} + g(z_i - z_e) = 0$$

$$-\frac{W_{cv}}{\dot{m}} + (h_i - h_e) = 0$$

$$W_{in} = -W_{cv}$$

26

Heat Exchanger (Boiler)

□ For System A or B, one at a time;

$$\frac{\dot{Q}_{cv}}{\dot{m}} - \frac{W_{cv}}{\dot{m}} + (h_i - h_e) + \frac{v_i^2 - v_e^2}{2} + g(z_i - z_e) = 0$$

$$\frac{\dot{Q}_{cv}}{\dot{m}} + (h_i - h_e) = 0$$

27

Heat Exchanger (Boiler)

□ For System A or B

$$\dot{Q}_{Ain} = -\dot{Q}_{Bout} = \dot{Q}_{cv}$$

$$\dot{m}_A(h_1 - h_2) = -\dot{m}_B(h_3 - h_4) = \dot{Q}_{cv}$$

$$\frac{\dot{m}_A}{\dot{m}_B} = \frac{h_1 - h_2}{h_4 - h_3}$$

28

Valve

$$\frac{\dot{Q}_{cv}}{\dot{m}} - \frac{W_{cv}}{\dot{m}} + (h_i - h_e) + \frac{v_i^2 - v_e^2}{2} + g(z_i - z_e) = 0$$

$$(h_i - h_e) = 0$$

$$\therefore h_i = h_e$$

29

Entropy

□ Entropy – Another Combination Property

Total Entropy S

$$dS = \frac{\delta Q}{T} \quad (\text{kJ/K})$$

Specific Entropy (per unit mass):

$$ds = \frac{\delta Q}{Tm} \quad (\text{kJ}/(\text{kg} \cdot \text{K}))$$

30

Control Volume Energy Analysis

□ **T-s diagram**

31

The Second Law of Thermodynamics

- It is known that a process must satisfy the first law to occur.
- However, satisfying the first law alone does not ensure that the process will actually take place.

32

The Second Law of Thermodynamics

FIGURE 1-3
Heat flows in the direction of decreasing temperature.

33

The Second Law of Thermodynamics

- **Clausius statement of the second law:**
 - It is impossible for any system to operate in such a way that the sole result would be an energy transfer by heat from a cooler to hotter body
 - The Clausius statement does not rule out the possibility of transferring energy by heat from a cooler body to a hotter body
 - The Clausius statement implies that it is impossible to construct a refrigeration cycle that operates without an input of work

34

The Second Law of Thermodynamics

- **Clausius statement of the second law:**
 - Refrigerators and Heat Pump in the next class

35

The Second Law of Thermodynamics

36

The Second Law of Thermodynamics

- **Kelvin-Planck statement of the second law:**
 - It is impossible for any system to operate in a thermodynamic cycle and deliver a net amount of energy by work to its surroundings while receiving energy by heat transfer from a single thermal reservoir.

37

Heat Engines

- That work can be converted to heat directly and completely, but converting heat to work requires the use of some special devices. These devices are called heat engines.

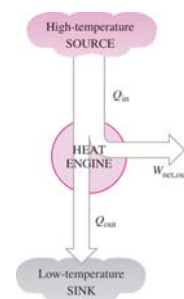
38

Heat Engines

- Heat engines differ considerably from one another, but all can be characterized by the following:
 - They receive heat from a high-temperature source
 - They convert part of this heat to work
 - They reject the remaining waste heat to a low-temperature sink
 - They operate on a cycle.

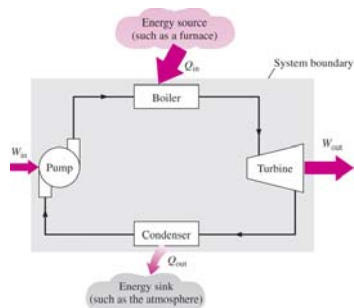
39

Heat Engines



40

Schematic of a Steam Power Plant



41

Steam Power Plant

- The various quantities shown on above figure are as follows:
 - Q_{in} = amount of heat supplied to steam in boiler from a high-temperature source
 - Q_{out} = amount of heat rejected from steam in condenser to low temperature sink
 - W_{out} = amount of work delivered by steam as it expands in turbine
 - W_{in} = amount of work required to compress water to boiler pressure

42

Steam Power Plant

- **The net work output:**

$$W_{net\ out} = W_{out} - W_{in}$$

$$W_{net\ out} = Q_{in} - Q_{out}$$
- **Thermal Efficiency:**

$$\text{Thermal efficiency} = \frac{\text{Net Work Output}}{\text{Total Heat Input}}$$

$$\eta = \frac{W_{net\ out}}{Q_{in}} = \frac{Q_{in} - Q_{out}}{Q_{in}} = 1 - \frac{Q_{out}}{Q_{in}}$$

43

The Quality of Energy

- **The Quality of Energy**
 - More of the high-temperature thermal energy can be converted to work. Therefore, the higher the temperature, the higher the quality of the energy

T_H , K	η_{th} , %
925	67.2
800	62.1
700	56.7
500	39.4
350	13.4

44

Vapor Power Plant

4.76 Figure P4.76 shows a simple vapor power plant operating at steady state with water circulating through the components. Relevant data at key locations are given on the figure. The mass flow rate of the water is 130 kg/s. Kinetic and potential energy effects are negligible. Determine

- (a) the heat transfer rate to the steam passing through the steam generator, in kW.
- (b) the net power developed for adiabatic operation of the turbine and pump, in kW.
- (c) the mass flow rate of the cooling water passing through the condenser, in kg/s, if the cooling water experiences a temperature rise of 15°C and a negligible pressure drop.

45

Vapor Power Plant

Figure P4.76
46

Rankine Cycle

- **Step 1: T-s Diagram**

7

Rankine Cycle

- **Step 2 Define the Properties**

State	T (°C)	P(Pa)	h (kJ/kg)	Phase
1	520*	10 M*	?	Superheated Vapor*
2	?	8 K*	?	x = 0.9 *
3	?	8 K*	?	Saturated Liquid*
4	80*	10 M*	?	Compressed Liquid*

- **Note: The data given is labeled by ***

48

Rankine Cycle

□ Step 2 Define the Properties

- State (1)
- It is in the superheated vapor region, and the temperature and pressure are given: $T = 520^{\circ}\text{C}$; $P = 10\text{MPa}$;
- h value can be determined from the superheated vapor table (Table A-6) by interpolation method.

49

Rankine Cycle

□ A partial list of Table A-6

T °C	$P = 9.0\text{ MPa (303.35}^{\circ}\text{C)}$				$P = 10.0\text{ MPa (311.00}^{\circ}\text{C)}$			
	v m^3/kg	u kJ/kg	h kJ/kg	s $\text{kJ/kg}\cdot\text{K}$	v m^3/kg	u kJ/kg	h kJ/kg	s $\text{kJ/kg}\cdot\text{K}$
Sat.	0.020489	2558.5	2742.9	5.6791	0.018028	2545.2	2725.5	5.6159
325	0.023284	2647.6	2857.1	5.8738	0.019877	2611.6	2810.3	5.7596
350	0.025816	2725.0	2957.3	6.0380	0.022440	2699.6	2924.0	5.9460
400	0.029960	2849.2	3118.8	6.2876	0.026436	2833.1	3097.5	6.2141
450	0.033524	2956.3	3258.0	6.4872	0.029782	2944.5	3242.4	6.4219
500	0.036793	3056.3	3387.4	6.6603	0.032811	3047.0	3375.1	6.5995
550	0.039885	3153.0	3512.0	6.8164	0.035655	3145.4	3502.0	6.7585
600	0.042861	3248.4	3634.1	6.9605	0.038378	3242.0	3625.8	6.9045
650	0.045755	3343.4	3755.2	7.0954	0.041018	3338.0	3748.1	7.0408
700	0.048589	3438.8	3876.1	7.2229	0.043597	3434.0	3870.0	7.1693
800	0.054132	3632.0	4119.2	7.4606	0.048629	3628.2	4114.5	7.4085
900	0.059562	3829.6	4365.7	7.6802	0.053547	3826.5	4352.0	7.6290
1000	0.064919	4032.4	4616.7	7.8855	0.058391	4029.9	4613.8	7.8349
1100	0.070224	4240.7	4872.7	8.0791	0.063183	4238.5	4870.3	8.0289
1200	0.075492	4454.2	5133.6	8.2625	0.067938	4452.4	5131.7	8.2126
1300	0.080733	4672.9	5399.5	8.4371	0.072667	4671.3	5398.0	8.3874

50

Rankine Cycle

□ Step 2 Define the Properties

- State (1) Cont'd
 - From Table A-6
- $T_1 = 500^{\circ}\text{C}$; $h_1 = 3375.1\text{ kJ/kg}$;
 $T_2 = 550^{\circ}\text{C}$; $h_2 = 3502.0\text{ kJ/kg}$;
 Therefore
 $T = 520^{\circ}\text{C}$;

$$h = h_1 + (T - T_1) \frac{h_2 - h_1}{T_2 - T_1}$$

$$= 3375.1 + (520 - 500) \left(\frac{3502.0 - 3375.1}{550 - 500} \right)$$

$$= 3425.86\text{ kJ/kg}$$

51

Rankine Cycle

□ Step 2 Define the Properties

State	T (°C)	P (Pa)	h (kJ/kg)	Phase
1	520*	10 M*	3425.86	Superheated Vapor*
2	?	8 K*	?	$x = 0.9$ *
3	?	8 K*	?	Saturated Liquid*
4	80*	10 M*	?	Compressed Liquid*

- Note: The data given is labeled by *

52

Rankine Cycle

□ Step 2 Define the Properties

- State (2)
- The quality x given to be $x = 0.9$, which implies that 90 percent of the mass is in the vapor phase and the remaining 10 percent is in the liquid phase. Therefore, we have saturated liquid-vapor mixture at a pressure 8 kPa.
- Then the temperature must be the saturation temperature at the given pressure by interpolation (Table A-5)

53

Rankine Cycle

□ A partial list of Table A-5

Press. kPa	Sat. Temp. T_{sat} °C	Specific volume, m^3/kg		Internal energy, kJ/kg			Enthalpy, kJ/kg			Entropy, kJ/kg·K		
		liquid, v_f	vapor, v_g	liquid, u_f	Evap., u_{fg}	vapor, u_g	liquid, h_f	Evap., h_{fg}	vapor, h_g	liquid, s_f	Evap., s_{fg}	vapor, s_g
1.0	6.97	0.001000	129.19	29.302	2355.2	2384.5	29.303	2484.4	2513.7	0.1059	8.8690	8.9749
1.5	13.02	0.001001	87.964	54.686	2338.1	2392.8	54.688	2470.1	2524.7	0.1956	8.6314	8.8270
2.0	17.50	0.001001	66.990	73.431	2325.5	2398.9	73.433	2459.5	2532.9	0.2606	8.4621	8.7227
2.5	21.08	0.001002	54.242	88.422	2315.4	2403.8	88.424	2451.0	2539.4	0.3118	8.3302	8.6421
3.0	24.08	0.001003	45.654	100.98	2306.9	2407.9	100.98	2443.9	2544.8	0.3543	8.2222	8.5765
4.0	28.96	0.001004	34.791	121.39	2293.1	2414.5	121.39	2432.3	2553.7	0.4224	8.0510	8.4734
5.0	32.87	0.001005	28.185	137.75	2282.1	2419.8	137.75	2425.0	2560.7	0.4762	7.9176	8.3938
7.5	40.29	0.001008	19.233	168.74	2261.1	2429.8	168.75	2405.3	2574.0	0.5763	7.6758	8.2501
10	45.81	0.001010	14.670	191.79	2245.4	2437.2	191.81	2392.1	2583.9	0.6492	7.4996	8.1488
15	53.97	0.001014	10.020	225.93	2222.1	2448.0	225.94	2372.3	2598.3	0.7549	7.2522	8.0071

54

Rankine Cycle

□ Step 2 Define the Properties

- State (2) Cont'd

• From Table A-5

$$P_1 = 7.5 \text{ kPa}; T_{sat1} = 40.29^\circ\text{C};$$

$$P_2 = 10 \text{ kPa}; T_{sat2} = 45.81^\circ\text{C};$$

Therefore

$$\text{If } P = 8 \text{ kPa};$$

$$\begin{aligned} T_{sat@8 \text{ kPa}} &= T_{sat1} + (P - P_1) \frac{T_{sat2} - T_{sat1}}{P_2 - P_1} \\ &= 40.29 + (8 - 7.5) \left(\frac{45.81 - 40.29}{10 - 7.5} \right) \\ &= 41.39^\circ\text{C}; \end{aligned}$$

55

Rankine Cycle

□ Step 2 Define the Properties

- State (2) Cont'd

$$P_1 = 7.5 \text{ kPa}; h_{f1} = 168.75 \text{ kJ/kg};$$

$$P_2 = 10 \text{ kPa}; h_{f2} = 191.81 \text{ kJ/kg};$$

Therefore

$$\text{If } P = 8 \text{ kPa};$$

$$\begin{aligned} h_{f@8 \text{ kPa}} &= h_{f1} + (P - P_1) \frac{h_{f2} - h_{f1}}{P_2 - P_1} \\ &= 168.75 + (8 - 7.5) \left(\frac{191.81 - 168.75}{10 - 7.5} \right) \\ &= 173.36 \text{ kJ/kg}; \end{aligned}$$

56

Rankine Cycle

□ Step 2 Define the Properties

- State (2) Cont'd

$$P_1 = 7.5 \text{ kPa}; h_{g1} = 2574.0 \text{ kJ/kg};$$

$$P_2 = 10 \text{ kPa}; h_{g2} = 2583.9 \text{ kJ/kg};$$

Therefore

$$\text{If } P = 8 \text{ kPa};$$

$$\begin{aligned} h_{g@8 \text{ kPa}} &= h_{g1} + (P - P_1) \frac{h_{g2} - h_{g1}}{P_2 - P_1} \\ &= 2574.0 + (8 - 7.5) \left(\frac{2583.9 - 2574.0}{10 - 7.5} \right) \\ &= 2575.8 \text{ kJ/kg}; \end{aligned}$$

57

Rankine Cycle

□ Step 2 Define the Properties

- State (2) Cont'd

• Then the average enthalpy of the mixture is

$$\begin{aligned} h_{@8 \text{ kPa}} &= h_{f@8 \text{ kPa}} + x h_{fg@8 \text{ kPa}} \\ &= h_{f@8 \text{ kPa}} + x (h_{g@8 \text{ kPa}} - h_{f@8 \text{ kPa}}) \\ &= 173.36 \text{ kJ/kg} + (0.9)(2575.8 \text{ kJ/kg} - 173.36 \text{ kJ/kg}) \\ &= 2335.56 \text{ kJ/kg} \end{aligned}$$

58

Rankine Cycle

□ Step 2 Define the Properties

State	T (°C)	P (Pa)	h (kJ/kg)	Phase
1	520*	10 M*	3425.86	Superheated Vapor*
2	41.39	8 K*	2335.56	x = 0.9 *
3	?	8 K*	?	Saturated Liquid*
4	80*	10 M*	?	Compressed Liquid*

□ Note: The data given is labeled by *

59

Rankine Cycle

□ Step 2 Define the Properties

- State (3)

• We have saturated liquid at specified pressure of 8 kPa. Then the temperature must be the saturation temperature at the given pressure, and the enthalpy must have the saturated liquid value:

60

Rankine Cycle

□ **Step 2 Define the Properties**

- **State (3) Cont'd**
- **From Table A-5**

$P_1 = 7.5 \text{ kPa}; T_{sat1} = 40.29^\circ\text{C};$
 $P_2 = 10 \text{ kPa}; T_{sat2} = 45.81^\circ\text{C};$

Therefore
 If $P = 8 \text{ kPa};$

$$T_{sat@8 \text{ kPa}} = T_{sat1} + (P - P_1) \frac{T_{sat2} - T_{sat1}}{P_2 - P_1}$$

$$= 40.29 + (8 - 7.5) \left(\frac{45.81 - 40.29}{10 - 7.5} \right)$$

$$= 41.39^\circ\text{C};$$

61

Rankine Cycle

□ **Step 2 Define the Properties**

- **State (3) Cont'd**

$P_1 = 7.5 \text{ kPa}; h_{f1} = 168.75 \text{ kJ/kg};$
 $P_2 = 10 \text{ kPa}; h_{f2} = 191.81 \text{ kJ/kg};$

Therefore
 If $P = 8 \text{ kPa};$

$$h_{f@8 \text{ kPa}} = h_{f1} + (P - P_1) \frac{h_{f2} - h_{f1}}{P_2 - P_1}$$

$$= 168.75 + (8 - 7.5) \left(\frac{191.81 - 168.75}{10 - 7.5} \right)$$

$$= 173.36 \text{ kJ/kg};$$

62

Rankine Cycle

□ **A partial list of Table A-5**

TABLE A-5
 Saturated water—Pressure table

Press., P kPa	Sat. temp., T _{sat} °C	Specific volume, m ³ /kg			Internal energy, kJ/kg			Enthalpy, kJ/kg			Entropy, kJ/kg·K		
		Sat. liquid, v _f	Sat. vapor, v _g	Sat. vapor, v _g	Sat. liquid, u _f	Evap., u _{fg}	Sat. vapor, u _g	Sat. liquid, h _f	Evap., h _{fg}	Sat. vapor, h _g	Sat. liquid, s _f	Evap., s _{fg}	Sat. vapor, s _g
1.0	6.97	0.001000	129.19	29.302	2355.2	2384.5	29.303	2484.4	2513.7	0.1059	8.8690	8.9749	
1.5	13.02	0.001001	87.964	54.866	2338.1	2392.8	54.868	2470.1	2524.7	0.1956	8.8314	8.9270	
2.0	17.50	0.001001	66.990	73.431	2325.5	2398.9	73.433	2459.5	2532.9	0.2606	8.8421	8.7227	
2.5	21.08	0.001002	54.242	88.422	2315.4	2403.8	88.424	2451.0	2539.4	0.3118	8.8302	8.6421	
3.0	24.08	0.001003	45.654	100.98	2306.9	2407.9	100.98	2443.9	2544.8	0.3543	8.8222	8.5765	
4.0	28.96	0.001004	34.791	121.39	2293.1	2414.5	121.39	2432.3	2553.7	0.4224	8.8510	8.4734	
5.0	32.87	0.001005	28.185	137.75	2282.1	2419.8	137.75	2423.0	2560.7	0.4762	7.9176	8.3938	
7.5	40.29	0.001008	19.233	168.74	2261.1	2429.8	168.75	2405.3	2574.0	0.5763	7.6738	8.2501	
10	45.81	0.001010	14.670	191.79	2245.4	2437.2	191.81	2392.1	2583.9	0.6492	7.4996	8.1488	
15	53.97	0.001014	10.020	225.93	2222.1	2448.0	225.94	2372.3	2598.3	0.7549	7.2522	8.0071	

63

Rankine Cycle

□ **Step 2 Define the Properties**

State	T (°C)	P(Pa)	h (kJ/kg)	Phase
1	520*	10 M*	3425.86	Superheated Vapor*
2	41.39	8 K*	2335.56	x = 0.9 *
3	41.39	8 K*	173.36	Saturated Liquid*
4	80*	10 M*	?	Compressed Liquid*

□ **Note: The data given is labeled by ***

64

Rankine Cycle

□ **Step 2 Define the Properties**

- **State (4)**
- **We have a compressed liquid**

$P = 10 \text{ Mpa}; T = 80^\circ\text{C};$

From Table A-7, we can get the enthalpy:

$$h_{@10 \text{ Mpa} \& 80^\circ\text{C}} = 342.94 \text{ kJ/kg};$$

65

Rankine Cycle

□ **A partial list of Table A-7**

TABLE A-7
 Compressed liquid water

T °C	P = 5 MPa (263.94°C)				P = 10 MPa (311.00°C)				P = 15 MPa (342.16°C)					
	v	u	h	s	v	u	h	s	v	u	h	s		
m ³ /kg	kJ/kg	kJ/kg	kJ/kg·K	m ³ /kg	kJ/kg	kJ/kg	kJ/kg·K	m ³ /kg	kJ/kg	kJ/kg	kJ/kg·K	m ³ /kg	kJ/kg	kJ/kg·K
Sat.	0.0012862	1148.1	1154.5	2.9207	0.0014522	1393.3	1407.9	3.3603	0.0016572	1585.5	1610.3	3.6848		
0	0.0009977	0.04	5.03	0.0001	0.0009952	0.12	10.07	0.0003	0.0009928	0.18	15.07	0.0004		
20	0.0009996	83.61	88.61	0.2954	0.0009973	83.31	93.28	0.2943	0.0009951	83.01	97.93	0.2932		
40	0.0010057	166.92	171.95	0.5705	0.0010035	166.33	176.37	0.5685	0.0010013	165.75	180.77	0.5666		
60	0.0010149	250.29	255.36	0.8287	0.0010127	249.43	259.55	0.8269	0.0010105	248.58	263.74	0.8234		
80	0.0010267	333.82	338.96	1.0723	0.0010244	332.69	342.90	1.0705	0.0010221	331.52	346.92	1.0689		
100	0.0010410	417.85	422.85	1.3034	0.0010385	416.23	426.62	1.2996	0.0010361	414.85	430.39	1.2958		
120	0.0010576	501.91	507.19	1.5236	0.0010549	500.18	510.73	1.5191	0.0010522	498.60	514.28	1.5148		
140	0.0010769	586.80	592.18	1.7344	0.0010738	584.72	595.45	1.7293	0.0010708	582.69	598.75	1.7243		
160	0.0010988	672.55	678.04	1.9374	0.0010954	670.06	681.01	1.9316	0.0010920	667.63	684.01	1.9259		
180	0.0011240	759.47	765.09	2.1338	0.0011200	756.48	767.48	2.1271	0.0011160	753.58	770.32	2.1206		
200	0.0011531	847.92	853.68	2.3251	0.0011482	844.32	855.80	2.3174	0.0011435	840.84	858.00	2.3100		
220	0.0011868	938.39	944.32	2.5127	0.0011809	934.01	945.82	2.5037	0.0011762	929.81	947.43	2.4951		
240	0.0012258	1031.6	1037.7	2.6983	0.0012192	1029.2	1038.3	2.6875	0.0012121	1021.0	1039.2	2.6774		
260	0.0012705	1128.5	1134.9	2.8841	0.0012653	1121.6	1134.3	2.8710	0.0012560	1115.3	1134.0	2.8586		
280					0.0013226	1221.8	1235.0	3.0565	0.0013095	1212.4	1233.0	3.0410		
300					0.0013980	1329.4	1343.3	3.2488	0.0013783	1317.6	1338.3	3.2279		
320									0.0014733	1431.9	1454.0	3.4263		
340									0.0015311	1527.9	1592.4	3.6595		

66

Rankine Cycle

□ **Step 2 Define the Properties**

State	T (°C)	P(Pa)	h (kJ/kg)	Phase
1	520*	10 M*	3425.86	Superheated Vapor*
2	41.39	8 K*	2335.56	x = 0.9 *
3	41.39	8 K*	173.36	Saturated Liquid*
4	80*	10 M*	342.94	Compressed Liquid*

□ **Note: The data given is labeled by ***

67

Rankine Cycle

□ **Step 3 Energy Analysis**

(a) **The heat transfer rate to the steam passing through the steam generator (Boiler)**

The mass flow rate of the water is given:

$$\dot{m}_s = 130 \text{ kg/s}$$

$$\dot{Q}_B = \dot{m}_s (h_1 - h_4)$$

$$= (130 \text{ kg/s})(3425.86 \text{ kJ/kg} - 342.94 \text{ kJ/kg})$$

$$= (130 \text{ kg/s})(3425.86 \text{ kJ/kg} - 342.94 \text{ kJ/kg})$$

$$= 400779.6 \text{ kJ/s}$$

$$= 400779.6 \text{ kW}$$

68

Rankine Cycle

□ **Step 3 Energy Analysis**

(b) **The net power developed for adiabatic operation of the turbine and pump in kW.**

The mass flow rate of the water is given: $\dot{m}_s = 130 \text{ kg/s}$

$$\dot{W}_{net\ out} = \dot{W}_T - \dot{W}_P$$

$$= \dot{m}_s [(h_1 - h_2) - (h_4 - h_3)]$$

$$= (130)[(3436 - 2336.8) - (342.8 - 173.4)]$$

$$= 120874 \text{ kJ/s}$$

$$= 120874 \text{ kW}$$

69

Rankine Cycle

□ **Step 3 Energy Analysis**

(c) **To determine the mass flow rate of the cooling water (\dot{m}_c) passing through the condenser in kg/s. if the cooling water experiences a temperature rise of 15 °C, and a negligible pressure drop.**

$$\dot{Q}_C = \dot{m}_s (h_2 - h_3)$$

$$\dot{Q} = \dot{m}_c C_p \Delta T$$

So:

$$\dot{m}_c = \frac{\dot{Q}_C}{C_p \Delta T} = \frac{\dot{m}_s (h_2 - h_3)}{C_p \Delta T}$$

70

Rankine Cycle

□ **Step 3 Energy Analysis**

(c) **cont'd:**

C_p is the specific heat of the water, which can be found in Table A-15.

$$C_p = \frac{4182 \text{ J}}{\text{kg} \cdot \text{C}} = \frac{4.182 \text{ kJ}}{\text{kg} \cdot \text{C}}$$

So:

$$\dot{m}_c = \frac{\dot{Q}_C}{C_p \Delta T} = \frac{\dot{m}_s (h_2 - h_3)}{C_p \Delta T} = \frac{(130)(2336.8 - 173.4)}{(4.182)(15)} = 4483.4 \text{ kg/s}$$

71

Rankine Cycle

□ **A partial list of Table A-15**

TABLE A-15
Properties of saturated water

Temp. T, °C	Saturation Pressure P _{sat} , kPa	Density ρ, kg/m ³		Enthalpy of Vaporization h _{fg} , kJ/kg		Specific Heat c _p , kJ/kg·K		Thermal Conductivity k, W/m·K		Dynamic Viscosity μ, kg/m·s		Prandtl Number Pr	Volume Expansion Coefficient β, 1/K
		Liquid	Vapor	Liquid	Vapor	Liquid	Vapor	Liquid	Vapor				
0.01	0.6113	999.8	0.0008	2501	4217	1864	0.561	0.0171	1.792 × 10 ⁻⁴	0.822 × 10 ⁻⁶	13.5	1.00	-0.006 × 10 ⁻³
5	0.8721	999.9	0.0008	2490	4205	1857	0.571	0.0173	1.519 × 10 ⁻⁴	0.834 × 10 ⁻⁶	11.2	1.00	0.015 × 10 ⁻³
10	1.2276	999.7	0.0008	2478	4194	1852	0.580	0.0176	1.307 × 10 ⁻⁴	0.846 × 10 ⁻⁶	9.45	1.00	0.733 × 10 ⁻³
15	1.7051	999.1	0.0010	2466	4180	1843	0.589	0.0179	1.138 × 10 ⁻⁴	0.859 × 10 ⁻⁶	8.29	1.00	0.538 × 10 ⁻³
20	2.339	998.0	0.0013	2454	4182	1847	0.598	0.0182	1.002 × 10 ⁻⁴	0.873 × 10 ⁻⁶	7.01	1.00	0.195 × 10 ⁻³
25	3.169	995.0	0.0017	2442	4180	1850	0.607	0.0186	0.891 × 10 ⁻⁴	0.887 × 10 ⁻⁶	6.14	1.00	0.287 × 10 ⁻³
30	4.246	996.0	0.0024	2431	4178	1875	0.615	0.0189	0.798 × 10 ⁻⁴	1.001 × 10 ⁻⁶	5.42	1.00	0.294 × 10 ⁻³
35	5.628	998.0	0.0037	2419	4178	1880	0.623	0.0192	0.720 × 10 ⁻⁴	1.016 × 10 ⁻⁶	4.83	1.00	0.237 × 10 ⁻³
40	7.384	992.1	0.0051	2407	4179	1885	0.631	0.0196	0.653 × 10 ⁻⁴	1.031 × 10 ⁻⁶	4.32	1.00	0.377 × 10 ⁻³

72

What is next?

- **Assignment 3 will be posted soon**
- **Continue on with Thermodynamics**

73