

MECH 262

ASSIGNMENT #3

MAXIME RICHARDS

8-98

GIVEN:

$T_{\infty} = 25^{\circ}\text{C}$

$h = 10 \text{ W}/(\text{m}^2 \cdot ^{\circ}\text{C})$

$T_F = 35^{\circ}\text{C}$

$T_i = 3^{\circ}\text{C}$

$T = 10^{\circ}\text{C}$

$C_p = 4190 \text{ J}/(\text{kg} \cdot ^{\circ}\text{C})$

$\rho = 1000 \text{ kg}/\text{m}^3$

* ASSUME FLOATING IN SPACE

$$\text{SURFACE AREA} = \frac{2\pi D^2}{4} + h\pi D \therefore = \frac{2\pi(0.06)^2}{4} + 0.125\pi(0.06)$$

$$\text{VOLUME} = \pi \frac{D^2}{4} \cdot h = \pi \frac{0.06^2}{4} \cdot 0.125 \quad V = 0.0003534 \text{ m}^3$$

$A_s = 0.0292 \text{ m}^2$

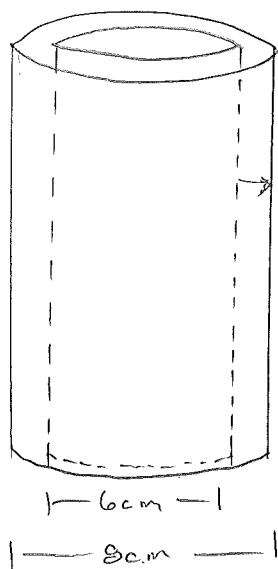
$$\frac{T - T_{\infty}}{T_i - T_{\infty}} = e\left(\frac{-hA_s}{\rho V C_p} \cdot t\right) \Rightarrow \ln\left(\frac{T - T_{\infty}}{T_i - T_{\infty}}\right) = \frac{-hA_s}{\rho V C_p} \cdot t$$

$$t = \ln\left(\frac{T - T_{\infty}}{T_i - T_{\infty}}\right) \cdot \frac{-\rho V C_p}{hA_s}$$

$$t = \ln\left(\frac{10 - 25}{3 - 25}\right) \cdot \frac{-(1000 \text{ kg}/\text{m}^3)(0.0003534 \text{ m}^3)(4190 \text{ J}/(\text{kg} \cdot ^{\circ}\text{C}))}{(10 \text{ W}/(\text{m}^2 \cdot ^{\circ}\text{C}))(0.0292 \text{ m}^2)}$$

$$t = 1942 \text{ s} \checkmark = 32.37 \text{ MINUTES}$$

IT TAKES ABOUT 32.37 MINUTES FOR THE CAN TO REACH 10°C



$$R_{\text{COND}} = \frac{\ln(r_2/r_1)}{2\pi k L}$$

$$R_{\text{CONV SIDE}} = \frac{1}{h \cdot 2\pi \cdot r \cdot L}$$

$$R_{\text{CONV TOP BOTTOM}} = \frac{1}{h A_s}$$

$L = 0.125 \text{ m}$

$r_2 = 0.04$

$r_1 = 0.03$

$k = 0.13 \text{ W}/(\text{m} \cdot ^{\circ}\text{C})$

$r = 0.04 \text{ m}$

$L = 0.125 \text{ m}$

$h = 10 \text{ W}/(\text{m}^2 \cdot ^{\circ}\text{C})$

$A_s = 2\pi r^2 = 0.00565 \text{ m}^2$

8-98 CONTINUED

$$\text{INS} \left\{ \begin{aligned} R_{\text{COND}} &= \frac{\ln(0.04/0.03)}{2\pi(0.13 \text{ W/m}\cdot\text{C}^\circ)(0.125 \text{ m})} = 2.82^\circ\text{C/W} \\ R_{\text{CONV}} &= \frac{1}{10 \text{ W/m}^2\cdot\text{C}^\circ(0.04 \text{ m})(0.125 \text{ m})2\pi} = 3.18^\circ\text{C/W} \end{aligned} \right.$$

$$\text{CAN} \left\{ \begin{aligned} R_{\text{CONV}} \\ \text{TOP BOTTOM} \end{aligned} \right. = \frac{1}{(10 \text{ W/m}^2\cdot\text{C}^\circ)(0.00565 \text{ m}^2)} = 17.7^\circ\text{C/W}$$

$$\frac{1}{R_o} = \frac{1}{R_{\text{CAN}}} + \frac{1}{R_{\text{COND}} + R_{\text{CONV}} \text{ INSULATION}} = \frac{1}{17.7} + \frac{1}{3.18 + 2.82}$$

$$R_o = \left[\frac{1}{R_o} \right]^{-1} = 4.48^\circ\text{C/W} \quad \checkmark$$

$$\tau = R_o \cdot C_T$$

$$\text{WHERE } C_T = \rho V C_p \\ = (1000)(0.0003534)(4190) = 1481$$

$$\tau = 4.48 \times 1481 = 6634$$

$$\frac{T - T_{\infty}}{T_i - T_{\infty}} = e^{-\frac{t}{\tau}} \Rightarrow \ln\left(\frac{T - T_{\infty}}{T_i - T_{\infty}}\right) = -\frac{t}{\tau}$$

$$t = -\tau \cdot \ln\left(\frac{T - T_{\infty}}{T_i - T_{\infty}}\right) = -6634 \cdot \ln\left(\frac{-15}{-22}\right) = 2540 \text{ s}$$

$$t = 42.35 \text{ MINUTES} \quad \checkmark$$

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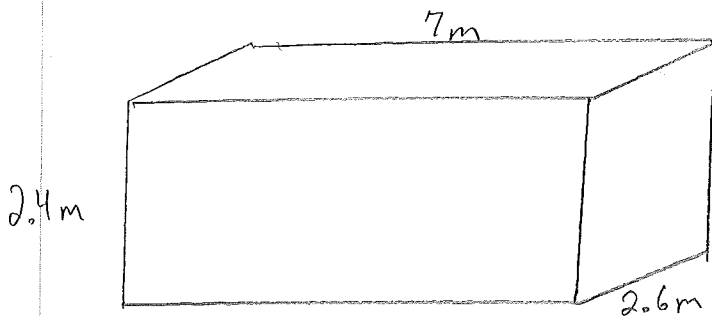
10-29

$$T_{\infty} = 30^{\circ}\text{C}$$

$$\text{VELOCITY } 85 \text{ km/h}$$

$$q_{\text{out}} = 663 \text{ kJ/minute}$$

ASSUME: $h_{\text{FRONT}} = h_{\text{REAR}} = h_{\text{SIDES}}$
ALL TURBULENT



FIND T_{AVG} FOR SURFACE OF TRUCK BOX

AIR AT 30°C

$$k = 0.02588 \text{ W/(m}\cdot^{\circ}\text{C)}$$

$$\nu = 1.608 \times 10^{-5} \text{ m}^2/\text{s}$$

$$Pr = 0.7282$$

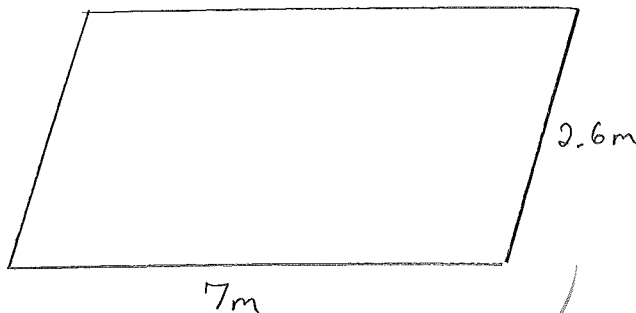
SOLUTION:

$$V = (85 \text{ km/h}) \left(\frac{1000 \text{ m}}{1 \text{ km}} \right) \left(\frac{1 \text{ hr}}{3600 \text{ s}} \right)$$

$$V = 23.61 \text{ m/s}$$

$$q_{\text{out}} = (663 \text{ kJ/minute}) \left(\frac{1 \text{ min}}{60 \text{ s}} \right)^{1/2}$$

$$q_{\text{out}} = 5.525 \text{ kW}$$



$$Re = \frac{VL}{\nu} = \frac{(23.61 \text{ m/s})(7 \text{ m})}{1.608 \times 10^{-5} \text{ m}^2/\text{s}}$$

$$Re = 10.278 \times 10^6$$

$$Nu_L = 0.037 Pr^{1/3} Re^{0.8} = 0.037 (0.7282)^{1/3} (10.278 \times 10^6)^{0.8}$$

$$Nu_L = 13546.034$$

$$h = Nu \frac{k}{L} = \frac{(13546.034)(0.02588 \text{ W/m}\cdot^{\circ}\text{C})}{(7 \text{ m})}$$

$$h = 50.08 \text{ W/(m}^2\cdot^{\circ}\text{C)}$$

TOTAL TRUCK AREA:

$$2(7)(2.6) + 2(2.6)(2.4) + 2(2.4)(7) = 82.48 \text{ m}^2$$

$$R_{\text{TOTAL}} = \frac{1}{h A_T} = \frac{1}{(50.08 \text{ W/m}^2\cdot^{\circ}\text{C})(82.48 \text{ m}^2)} = 2.42 \times 10^{-4} \text{ }^{\circ}\text{C/W}$$

10.29 CONTINUED...

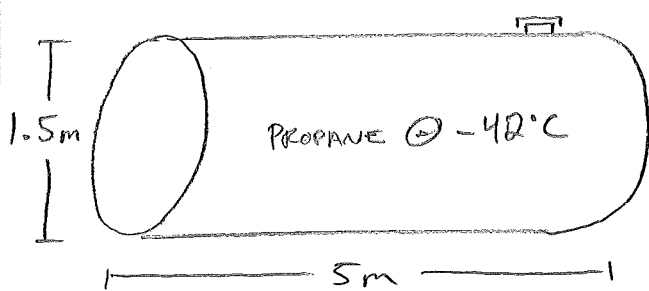
$$q = \frac{\Delta T}{R} = \frac{T_{\infty} - T_{\text{TRUCK}}}{R}$$

$$T_{\text{TRUCK}} = T_{\infty} - q \cdot R = 30^{\circ}\text{C} - (5525 \text{ W}) (2.42 \times 10^{-4} \text{ }^{\circ}\text{C/W})$$

$$T_{\text{TRUCK}} = 28.66^{\circ}\text{C} \quad \checkmark$$

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11-38 GIVEN:



$$T_{\infty} = 25^{\circ}\text{C}$$

$$\text{VOLUME} = \frac{\pi D^2 L}{4} = \frac{\pi (1.5)^2 (5)}{4}$$

$$V = 8.836 \text{ m}^3 \quad T_{\text{AVG}} = -8.5^{\circ}\text{C}$$

$$P_R = \alpha T_{\text{AVG}} = 0.7387$$

$$\text{PROPANE } \rho = 581 \text{ kg/m}^3$$

$$H_{\text{VAP}} = 425 \text{ kJ/kg}$$

$$T_{\text{BOIL}} = -42^{\circ}\text{C}$$

$$\rho_{\text{AIR}} = 1.341 \text{ kg/m}^3$$

$$(581 \text{ kg/m}^3)(8.836 \text{ m}^3) = 5133.72 \text{ kg}$$

AMOUNT OF PROPANE IN TANK

$$M_{\text{PROPANE}} = 5133.72 \text{ kg}$$

$$H_{\text{VAP}} = (425 \text{ kJ/kg})(5133.72 \text{ kg}) = 2.18 \times 10^6 \text{ kJ TO}$$

EMPTY TANK

$$\mu = 1.68 \times 10^{-5} \text{ kg/m}\cdot\text{s}$$

$$\beta = \frac{1}{T_{\text{AVG}} \text{ } ^{\circ}\text{K}} = \frac{1}{264.5}$$

$$\beta = 0.00378$$

$$GR = \frac{g \beta (T_{\text{BOIL}} - T_{\infty}) D^3 \rho^2}{\mu^2}$$

$$GR = \frac{(9.81)(0.00378)(67)(1.5)^3(1.341)^2}{(1.68 \times 10^{-5})^2}$$

$$GR = 5.3425 \times 10^{10}$$

$$GR PR = (5.3425 \times 10^{10})(0.7387)$$

$$GR PR = 3.95 \times 10^{10}$$

$$K_{\text{FORM TABLE}} = 0.02288 \frac{\text{W}}{\text{m}^2 \cdot ^{\circ}\text{C}} \therefore C = 0.13 \text{ AND } n = 1/3$$

$$Nu = C (GR PR)^n = 0.13 (3.95 \times 10^{10})^{1/3} = 442.7$$

$$h = \frac{Nu k}{D} = \frac{(442.7)(0.02288 \text{ W/m}^2 \cdot ^{\circ}\text{C})}{1.5 \text{ m}} = 6.753 \text{ W/m}^2 \cdot ^{\circ}\text{C}$$

$$q = h A \Delta T = (6.753 \text{ W/m}^2 \cdot ^{\circ}\text{C}) \left(2\pi(0.75^2) + \pi(1.5)(5) \right) (67)^{\circ}\text{C}$$

$$q = 12259.7 \text{ W}$$

$$t = \frac{H_{\text{VAP}}}{q} = \frac{2.18 \times 10^9 \text{ J}}{12259.7 \text{ J/s}} = 177818 \text{ s}$$

$t = 49.4 \text{ HOURS FOR TANK TO EMPTY}$ ✓

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