

Mech 262
Assignment #4
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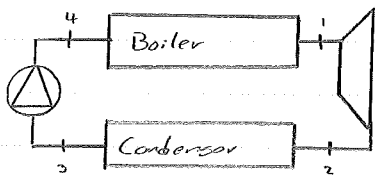
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#1

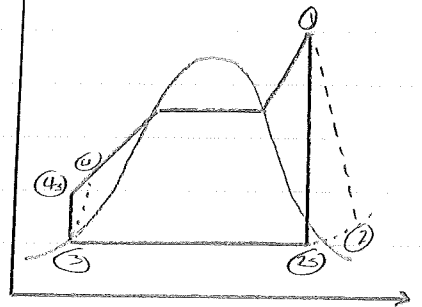
Given: A Rankine Cycle producing $100 \times 10^6 \text{ W}$



$P_1 = 15 \text{ MPa}$, $T_1 = 600^\circ\text{C}$, $P_2 = 10 \text{ kPa}$, $\eta = 0.85$, $P_{4-1} = 5\%$

- Find:
- Thermal Efficiency
 - Mass flow rate (kg/s)
 - Back work ratio (W_P/W_T)

State	T(°C)	P(kPa)	v	h	s	Cond
1	600*	15000*		3582.3	6.6776	Super
2s		10*		2114.92	6.6776	
2		10		2335.03		
3		10	0.00101	191.83	0.6493	Sat. Liq.
4s		15750		207.73	0.6493	
4		15750		210.54		



h_1 and s_1 from table A-6 given T_1 and P_1 , $P_2 = P_{2s} = P_1$, $P_4 = (105\%)(P_3) = 15750$, $s_{2s} = s_1$

$$\eta_T = \frac{h_1 - h_{2s}}{h_1 - h_{2s}} \Rightarrow \eta_T (h_1 - h_{2s}) = h_1 - h_2 \Rightarrow h_2 = h_1 - \eta_T (h_1 - h_{2s}) = 3582.3 - 0.85(3582.3 - 2114.92) = 2335.03$$

$$x_2 = \frac{s_2 - s_f}{s_g - s_f} = \frac{6.6776 - 0.6493}{8.1502 - 0.6493} = 0.803677 \quad h_{2s} = h_f + x_2(h_g - h_f) = 191.83 + (0.803677)(2584.7 - 191.83) = 2114.92$$

h_3, s_3 and v_3 from table A-5 given P_3 , $h_{4s} = h_3 + v_3 \Delta P = 191.83 + 0.00101(15750 - 10) = 207.73$

$$s_{4s} = s_3 \quad \eta_P = \frac{h_{4s} - h_3}{h_4 - h_3} \quad h_4 - h_3 = \frac{h_{4s} - h_3}{\eta_P} \quad h_4 = h_3 + \frac{h_{4s} - h_3}{\eta_P} = 191.83 + \frac{207.73 - 191.83}{0.85} = 210.536$$

$$\eta = \frac{W_{out}}{Q_{in}} = \frac{(h_1 - h_2) - (h_4 - h_3)}{h_1 - h_4} = \frac{(3582.3 - 2335.03) - (210.54 - 191.83)}{(3582.3 - 210.54)} = 0.3644 = \boxed{36.44\%}$$

$$W_{net} = W_{Turb} - W_{Pump} = \dot{m}(h_1 - h_2) - \dot{m}(h_4 - h_3) \rightarrow \dot{m} = \frac{W_{net}}{(h_1 - h_2) - (h_4 - h_3)}$$

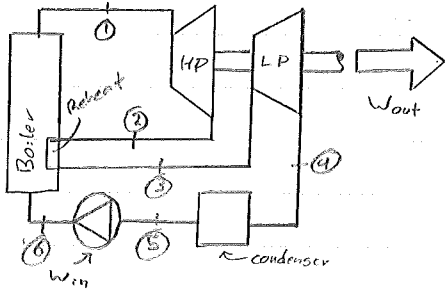
$$\dot{m} = \frac{100 \times 10^6}{(3582.3 - 2335.03) - (210.54 - 191.83)} = 81396.1 \text{ kg/s} = \boxed{2.93 \times 10^8 \text{ kg/h}}$$

$$BWR = \frac{W_P}{W_T} = \frac{\dot{m}(h_4 - h_3)}{\dot{m}(h_1 - h_2)} = \frac{210.54 - 191.83}{3582.3 - 2335.03} = \boxed{0.015}$$

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#2

Given: A Rankine Cycle:



$$P_1 = 9 \text{ MPa} \quad T_1 = 600^\circ\text{C} \quad T_3 = 500^\circ\text{C}$$

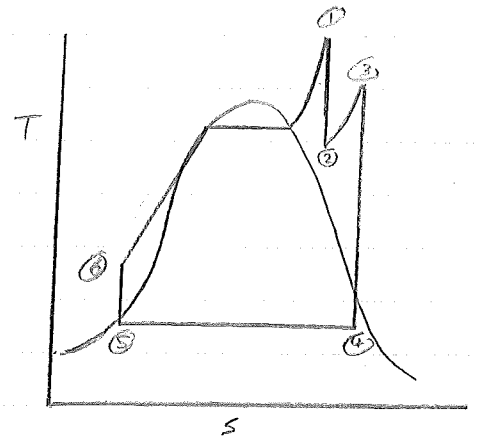
$$P_4 = 7.5 \text{ kPa} \quad \dot{m} = 150 \text{ kg/s}$$

Find: a) Net Power,

b) Rate of heat transfer to working fluid in the reheat process

c) Thermal Efficiency d) Rate of heat transfer if reheat to 550°C

State	T (°C)	P (kPa)	v	h	s	Cond
1	600*	9000*		3633.7	6.9589	Super
2	138.88	331.4		2729.87	6.9589	Sat Vapor
3	500*	331.4		3485.65	8.2831	Super
4		7.5*		2584.1	8.2831	
5	40.29	7.5	0.001008	168.79	0.5764	Sat Liquid
6		9000		177.854		



$$P_6 = P_1, P_5 = P_4, h_1 \text{ and } s_1 \text{ from Table A-6 given } T_1 \text{ and } P_1, s_2 = s_1$$

$$\text{Since } \textcircled{2} \text{ is saturated vapor } T_2, P_2 \text{ and } h_2 \text{ interpolated from table A-5 given } s_2, P_3 = P_2$$

$$\text{Given } T_3 \text{ and } P_3, \text{ interpolate from Table A-6 to find } h_3 \text{ and } s_3, s_4 = s_3$$

$$x_4 = \frac{s_4 - s_f}{s_g - s_f} = \frac{8.2831 - 0.5764}{8.2515 - 0.5764} = 1.004 \quad h = h_f + x(h_g - h_f) = 168.79 + (1.004)(2574.8 - 168.79) = 2584.71$$

$$\text{Since } \textcircled{5} \text{ is saturated liquid } T_5, h_5 \text{ and } s_5 \text{ from Table A-5}$$

$$h_6 = h_5 + v_5 \Delta P = 168.79 + 0.001008(9000 - 7.5) = 177.854$$

$$\dot{W}_{\text{net}} = \dot{V}_{\text{HP}} + \dot{V}_{\text{LP}} - \dot{V}_{\text{P}} = \dot{m} [(h_1 - h_2) + (h_3 - h_4) - (h_6 - h_5)] = 150 [(3633.7 - 2729.87) + (3485.65 - 2584.1) - (177.854 - 168.79)] = 269447 \text{ kJ/s} = \boxed{269.4 \text{ MW}}$$

$$\dot{Q} = \dot{m} (h_2 - h_1) = 150 (3485.65 - 2729.87) = \boxed{113367 \text{ kJ/s}}$$

$$\eta = \frac{(h_1 - h_2) + (h_3 - h_4) - (h_6 - h_5)}{(h_1 - h_6) + (h_3 - h_2)} = \frac{(3633.7 - 2729.87) + (3485.65 - 2584.1) - (177.854 - 168.79)}{(3633.7 - 177.854) + (3485.65 - 2729.87)} = 0.4895 = 48.95\%$$

$$= \boxed{48.95\%}$$

#2 cont...

State	T	P	v	h	s	Cond
✓ 1	600 *	9000 *		3633.7	6.9589	Super
✓ 2	138.88	331.4		2729.87	6.9589	Sat Vapor
3	550 *	331.4		3594.3	8.54731	Super
4		7.5 *		2667.53	8.54731	
✓ 5	40.29	7.5	0.001008	168.79	0.5764	Sat Liquid
✓ 6		9000		177.054		

Data for states
 ①, ②, ⑤ cond ③ given

Given P_2 and T_2 interpolate from Table A-6 to find

500	3486.0	8.3251		500	3484.9	8.1913	300	3594.6	8.5897
(0.30) 550	3594.8	8.5897	(0.40) →	550	3593.15	8.4558	331.4	3594.3	8.54731
600	3703.2	8.5897		600	3707.4	8.4558	400	3593.15	8.4558

$$s_4 = s_3 \quad x_4 = \frac{s_4 - s_f}{s_g - s_f} = \frac{8.54731 - 0.5764}{8.2515 - 0.5764} = 1.03854$$

$$h_4 = h_f + x(h_g - h_f) = 168.79 + 1.03854(2576.8 - 168.79) = 2667.53$$

$$\dot{Q} = \dot{m}(h_3 - h_2) = 150(3594.3 - 2729.87) = \boxed{129665 \text{ kJ/s}}$$

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